

NOTES: What do you know about solving systems of equations?

1. What is a system of equations?

two or more equations working together

2. Three possible solutions for a system of equations:

- one solution
- two or more
- no solution

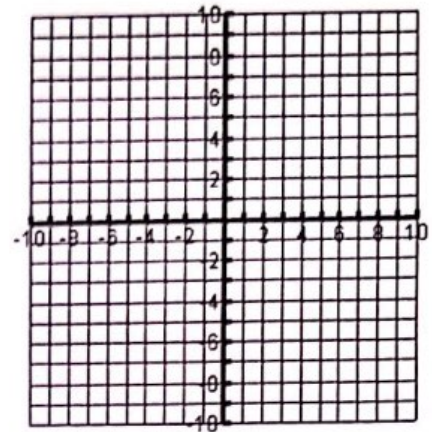
3. Three ways to solve a system of equations:

- graphing
- substitution
- eliminate

4. Solve by graphing:

$$x + y = 10$$

$$x - y = 4$$



5. Solve by substitution:

$$3x + y = -9$$

$$-3x - 2y = 12$$

6. Solve by elimination:

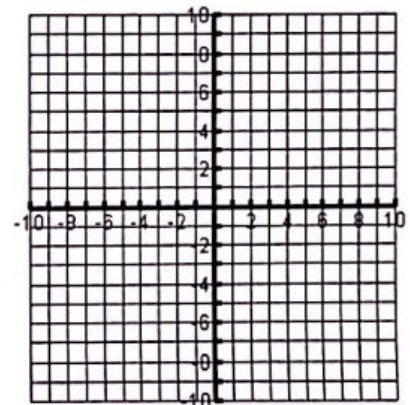
$$2x + 4y = -4$$

$$3x + 5y = -3$$

7. Solve by graphing:

$$y > \frac{2}{3}x + 2$$

$$y < \frac{2}{3}x - 1$$



Method 1: Graphing

- Solve each equation for y.
- Enter the first equation into Y₁.
- Enter the second equation into Y₂.
- Use the **INTERSECT** option to find where the two graphs intersect (the answer).
 2nd TRACE (CALC) #5 intersect
 Move spider close to the intersection.
 Hit **ENTER** 3 times.

EX1: Solve $4x - 6y = 12$
 $2x + 2y = 6$

$$\begin{array}{r} 4x - 6y = 12 \\ -4x = -4x \end{array} \quad \rightarrow \quad \begin{array}{r} y = \frac{2}{3}x - 2 \\ \hline 2x + 2y = 6 \\ -2x = -2x \end{array}$$

$$\frac{-6y}{-6} = \frac{-4x + 12}{-6} \quad \rightarrow \quad \frac{2y}{2} = \frac{-2x + 6}{2} \rightarrow y = -x + 3$$

(3, 0)

EX2: There are 25 bikes and trikes at the park. The bikes and trikes have 60 wheels in all. How many bikes and trikes are in the park?

x: bike
y: trike

$$\begin{array}{r} x + y = 25 \\ -x = -x \end{array} \quad \rightarrow \quad \begin{array}{r} 2x + 3y = 60 \\ -2x = -2x \end{array}$$

$$y = -x + 25 \quad \rightarrow \quad \frac{3y}{3} = \frac{-2x + 60}{3} \rightarrow y = \frac{2}{3}x + 20$$

(15, 10)
 15 bikes
 10 trikes

You try!! Solve by graphing. (You can do these by hand or with a calculator!)

1. $-3x + 2y = 8$
 $x + 2y = -8$

$$y = \frac{3x + 8}{2}$$

$$y = \frac{-x - 8}{2}$$

(-4, -2)

2. $-2x + 4y = 6$
 $4x - 8y = 12$

$$y = \frac{2x + 6}{4}$$

$$y = \frac{-4x + 12}{-8}$$

no solution

3. $2x - y = 3$
 $6x - 3y = 9$

$$y = \frac{-2x + 3}{-1}$$

$$y = \frac{-6x + 9}{-3}$$

infinite solutions

4. $y = (x + 3)^2$
 $y = -2x + 9$

(0, 9)
(-8, 25)

5. $9y - x = 41$
 $y = |x + 1|$

math num abs(
 $y = \frac{x + 41}{9}$

(-5, 4)
(4, 5)

6. $y + 6 = |x + 5|$
 $\frac{1-y}{3} = \left| \frac{1}{4}x \right|$

$$y = -6 + |x + 5|$$

$$y = -3 \left| \frac{1}{4}x \right| + 1$$

(-6.86, -4.14)
(1.14, 0.14)

Method 2: Substitution

- Solve one of the equations for either $x =$ or $y =$
- Replace this value in the other equation
- Solve this new equation
- Place this numerical value into either of the ORIGINAL equations in order to solve for the other variable
- Write solution as a POINT

EX3: $2x - 3y = -2$
 $4x + y = 24$

$$\begin{array}{r} 4x + y = 24 \\ -4x = \\ \hline y = -4x + 24 \end{array}$$

$(5, 4)$

$$\begin{array}{r} 2x - 3(-4x + 24) = -2 \\ 2x + 12x - 72 = -2 \\ +72 \\ \hline 14x = 70 \\ \frac{14x}{14} = \frac{70}{14} \\ x = 5 \end{array}$$

EX4: $x + 3y = -9$
 $5x + 8y = 11$

$$\begin{array}{r} x + 3y = -9 \\ -3y = \\ \hline x = -3y - 9 \end{array}$$

$$\begin{array}{r} 5(-3y - 9) + 8y = 11 \\ -15y - 45 + 8y = 11 \\ +45 \\ \hline -7y = 56 \\ \frac{-7y}{-7} = \frac{56}{-7} \\ y = -8 \end{array}$$

$x + 3(-8) = -9$
 $x - 24 = -9$
 $x = 15$

$(15, -8)$

EX5: Jake's Surf Shop rents surfboards for \$6.00 plus \$3.00 per hour. Rita's rents them for \$9.00 plus \$2.50 per hour.

a. After how many hours of surfing will the rental fee be the same for both surf shops?

x : hours
 y : cost

$y = 6 + 3x$ ← Jake's
 $y = 9 + 2.5x$ ← Rita's

$$\begin{array}{r} 6 + 3x = 9 + 2.5x \\ -6 = \\ \hline \frac{1}{2}x = 3 \\ x = 6 \end{array}$$

(6 hours)

b. You only want to surf for 2 hours; which surf shop should you go to?

$y = 6 + 3(2)$

$y = \$12$
Jake's!

$y = 9 + 2.5(2)$

$y = \$14$

You try!! Solve using substitution.

1. $x - 2y = 13$
 $3x + 2y = 15$

$(7, -3)$

2. $4x + 5y = -14$
 $8x + 10y = -20$

no solution

Method 3: Elimination

Basic Goal: Add the two equations together so that the x or y is eliminated.

- Arrange equations so variables, equal signs, and constants line up vertically.
- Multiply one or both equations by a value so that one variable in the 1st equation has the opposite coefficient in the other equation.
- Add the two equations.
- Solve for the remaining variable.
- Substitute solution from step 4 into either equation and solve for the remaining variable.

EX6: $x - 2y = 12$
 $5y = 6x - 23$

$$\begin{array}{r} x - 2y = 12 \quad (6) \\ -6x + 5y = -23 \quad (+) \\ \hline -7y = 49 \\ \hline y = -7 \end{array}$$

Substitution: $x - 2(-7) = 12$
 $x - 14 = 12$
 $x = 26$

Solution: $(26, -7)$

EX7: A jar filled with nickels and quarters contains a total of 55 coins. The value of all the coins in the jar is \$6.95. How many quarters are in the jar?

n : nickels
 q : quarters

$$\begin{array}{r} (n + q = 55) \quad (0.25) \\ 0.05n + 0.25q = 6.95 \quad (-) \\ \hline 0.2n + 0.25q = 13.75 \\ -0.05n + 0.25q = -6.95 \\ \hline 0.2n = 6.8 \\ \hline n = 34 \end{array}$$

Substitution: $34 + q = 55$
 $q = 21$ quarters

You try!! Solve using elimination.

1. $2x + 8y = 6$
 $-5x - 20y = -15$

2. $5x + 4y = -14$
 $3x + 6y = 6$

3. The Algebra 2 classes took 60 minutes to answer a combination of 20 multiple-choice and extended-response questions. The class took 2 minutes to answer each multiple choice question and 6 minutes to answer each extended-response question. How many of each type of questions was on the test?