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## Math 3 Honors Unit 4: Rational Expressions

## EVERY TIME YOU DO THIS:


$f_{6 \times 1}=\frac{x+2 x+t}{x+3}$
$=\frac{2 x+1}{3}$
A KITTEN DIES.

| Monday | Tuesday | Wednesday | Thursday | Friday |
| :---: | :---: | :---: | :---: | :---: |
| March 4 <br> - Simplify rational expressions <br> HW: worksheet 4.1 | March 5 <br> - Multiply and divide rational expressions <br> HW: worksheet 4.2 | March 6 <br> - Add and subtract rational expressions <br> HW: worksheet 4.3 | March 7 <br> - Add and subtract rational expressions <br> HW: worksheet 4.4 | March 8 <br> - QUIZ!! <br> - Solve rational equations <br> HW: worksheet 4.5 |
| March 11 <br> - Solve rational equations <br> HW: worksheet 4.6 | March 12 <br> - Graph rational functions <br> HW: worksheet 4.7 | March 13 <br> - Graph rational functions <br> HW: worksheet 4.8 | March 14 <br> - Review for test <br> HW: finish review | March 15 <br> - TEST!! |

## 6.1-Simplify Rational Expressions

Factor completely.

1. $75 x^{4}-48 y^{4}$
2. $3 x^{2}+10 x+8$
3. $x^{2}+4 x y-12 y^{2}$
4. $12 x^{3}-12 x^{2}-9 x$

Simplify the following rational expressions. State any restrictions on the variables.
5. $\frac{4 x+6}{2 x+3}$
6. $\frac{2 y}{y^{2}+6 y}$
7. $\frac{20+40 x}{20 x}$
8. $\frac{7 x-28}{x^{2}-16}$
9. $\frac{3 y^{2}-3}{y^{2}-1}$
10. $\frac{3 x^{2}-12}{x^{2}-x-6}$
11. $\frac{x^{2}+3 x-18}{x^{2}-36}$
12. $\frac{x^{2}+13 x+40}{x^{2}-2 x-35}$

## 6.2 - Multiply and Divide Rational Expressions

Simplify the following rational expressions. State any restrictions on the variables.

1. $\frac{y^{2}-2 y}{y^{2}+7 y-18} \div \frac{y^{2}-11 y+18}{y^{2}-81}$
2. $\frac{y^{2}-25}{y^{2}-16} \div \frac{2 y+10}{y^{2}-4 y}$
3. $\frac{14 x+7}{4 x-6} \cdot \frac{8 x-12}{42 x+21}$
4. $\frac{x^{2}}{x^{2}+2 x+1} \div \frac{3 x}{x^{2}-1}$
5. $\frac{2 x+4}{3 x-3} \cdot \frac{12 x-12}{x+5}$
6. $\frac{\frac{1}{3 x}}{\frac{5}{6 y}}$
7. $\frac{x-2}{(x+2)^{2}} \cdot \frac{x+2}{2 x-4}$
8. $\frac{5 a}{5 a+5} \cdot \frac{10 a+10}{a}$
9. $\frac{x+6}{x^{2}-36}$

## 6.3 - Add and Subtract Rational Expressions

Simplify the following rational expressions. State any restrictions on the variables.

1. $\frac{8}{3 x^{3} y}+\frac{4}{9 x y^{3}}$
2. $3 x-\frac{x^{2}-5 x}{x^{2}-2}$
3. $\frac{5 x}{2 y+4}-\frac{6}{y^{2}+2 y}$
4. $\frac{7}{5 y+25}-\frac{4}{3 y+15}$
5. $\frac{7}{2 x y^{2}}+\frac{3}{8 x^{2} y}$
6. $\frac{6 y-4}{y^{2}-5}+\frac{3 y+1}{y^{2}-5}$
7. $\frac{x+2}{x^{2}+4 x+4}+\frac{2}{x+2}$
8. $\frac{x^{2}}{5}+\frac{x^{2}}{5}$
9. $\frac{y}{4 y+8}-\frac{1}{y^{2}+2 y}$

## 6.4 - Simplify Rational Expressions

Simplify the following rational expressions. State any restrictions on the variables.

1. $\frac{1+\frac{2}{x}}{4-\frac{6}{x}}$
2. $\frac{x^{2}-6 x}{x^{2}-36} \cdot \frac{x+6}{x^{2}}$
3. $-\frac{2}{n+4}-\frac{n^{2}}{n^{2}-16}$
4. $\frac{4}{x^{2}-25}+\frac{6}{x^{2}+6 x+5}$
5. $\frac{d^{2}+2 d-35}{d^{2}-10 d+25} \div \frac{d^{2}-49}{d^{2}+d-30}$
6. $\frac{\frac{2}{y}-1}{\frac{3}{x}+1}$
7. $\frac{4}{x^{2}-16}+\frac{5}{x-5}-\frac{4}{x+4}$
8. $\frac{x+1}{2 x^{2}}-\frac{2 x-2}{9 x}+\frac{5 x}{12}$
9. $3+\frac{r}{3+\frac{3}{3+r}}$

## 6.5-Solve Rational Expressions

Solve for the variable.

1. $\frac{3-x}{6}=\frac{6-x}{12}$
2. $\frac{2}{6 x+2}=\frac{x}{3 x^{2}+11}$
3. $\frac{3}{2 x-4}=\frac{5}{3 x+7}$
4. $\frac{2}{x+2}+\frac{5}{x-2}=\frac{6}{x^{2}-4}$
5. $\frac{7}{x^{2}-5 x}+\frac{2}{x}=\frac{3}{2 x-10}$
6. $\frac{1}{4-5 x}=\frac{3}{x+9}$
7. $\frac{7}{2}=\frac{7 x}{8}-4$
8. $4+\frac{2 y}{y-5}=\frac{8}{y-5}$

## 6.6 - More Solve Rational Expressions

Solve for the variable.

1. $\frac{9}{3 x}=\frac{4}{x+2}$
2. $\frac{8}{3 x-2}=\frac{2}{x-1}$
3. $\frac{x-3}{x+5}=\frac{x}{x+2}$
4. $\frac{4(x-4)}{x^{2}+2 x-8}=\frac{4}{x+4}$
5. $\frac{2}{3 x}+\frac{1}{6}=\frac{4}{3 x}$
6. $\frac{2}{x-3}+\frac{1}{x}=\frac{x-1}{x-3}$
6.7-Graphs of Rational Functions

Identify points of discontinuity, holes, vertical asymptotes, x-intercepts, and horizontal asymptote of each.

1. $f(x)=\frac{1}{3 x^{2}+3 x-18}$
2. $f(x)=\frac{x-2}{x-4}$
3. $f(x)=\frac{x^{3}-x^{2}-6 x}{-3 x^{2}-3 x+18}$
4. $f(x)=\frac{x^{2}+x-6}{-4 x^{2}-16 x-12}$

Identify points of discontinuity, holes, vertical asymptotes, x-intercepts, and horizontal asymptote of each. Then sketch the graph.
5. $f(x)=-\frac{4}{x^{2}-3 x}$

7. $f(x)=\frac{x+4}{-2 x-6}$

6. $f(x)=\frac{x-4}{-4 x-16}$

8. $f(x)=\frac{x^{3}-9 x}{3 x^{2}-6 x-9}$


## 6.8-More Graphs of Rational Functions

Identify points of discontinuity, holes, vertical asymptotes, x-intercepts, and horizontal asymptote of each. Then sketch the graph.

1. $f(x)=\frac{3 x^{2}-12 x}{x^{2}-2 x-3}$

2. $f(x)=\frac{2}{x^{2}+3 x-10}$

3. $f(x)=\frac{x+2}{2 x+6}$

4. $f(x)=\frac{x^{2}-4 x+3}{x^{2}-x-6}$


Answer the following multiple choice questions.
5. Which value of x will make the fraction $\frac{x-3}{x+6}$ undefined?
A 6
B - 6
C 3
D - 3
6. Which of the following is the equation of an asymptote for the function graphed?

A $x=-4$
B $y=0$
C $x=4$
D $y=4$

7. What value(s) are restricted from the range of $f(x)$ ?

A 1
B 0
C 3
D no restricted values

8. A value of x that makes the expression $\frac{x^{2}+4 x-12}{x^{2}-2 x-15}$ undefined is
A -6
B -2
C 3
D 5
9. The graph of the function $y=\frac{8}{x}$ lies in what quadrant(s)?
A QI and QIII
B QII and QIV
C QII
D QIII

